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The Virtual Learning Environment for Computer Programming

## Adding fingers

P55691_en
Divuitè Concurs de Programació de la UPC - Final (2020-10-07)
Consider a game for two players playing alternatively. Both players show a certain number of fingers in each hand. Let $X$ be the player that moves next, and let $Y$ be the other player. Let $a$ and $b$ be the number of fingers shown by X , and let $c$ and $d$ be the number of fingers shown by Y. In each turn, these are the allowed moves:

1. Add mod 5 as many fingers as $X$ has in a non-empty hand (a hand showing at least one finger) to one of Y 's non-empty hands. That is:

$$
\begin{cases}(a, b)(c, d) \rightarrow(a, b)(c+a, d) & \text { if } a, c \neq 0 \\ (a, b)(c, d) \rightarrow(a, b)(c, d+a) & \text { if } a, d \neq 0 \\ (a, b)(c, d) \rightarrow(a, b)(c+b, d) & \text { if } b, c \neq 0 \\ (a, b)(c, d) \rightarrow(a, b)(c, d+b) & \text { if } b, d \neq 0\end{cases}
$$

2. "Move" the fingers in one of $X$ 's hands to the other hand, provided that none of them are empty. Again, the operations are made mod 5:

$$
\begin{cases}(a, b)(c, d) \rightarrow(a+b, 0)(c, d) & \text { if } a, b \neq 0 \\ (a, b)(c, d) \rightarrow(0, a+b)(c, d) & \text { if } a, b \neq 0\end{cases}
$$

3. "Redistribute" the fingers in X's hands, if one of them is empty:

$$
\begin{cases}(a, 0)(c, d) \rightarrow(x, y)(c, d) & \text { if } x+y=a \text { and } 0<x, y<a \\ (0, b)(c, d) \rightarrow(x, y)(c, d) & \text { if } x+y=b \text { and } 0<x, y<b\end{cases}
$$

Both players play perfectly. The first player to get to $(0,0)$ loses the game. A game that never ends is considered to be a draw.

## Input

Input consists of several cases, each one with $a, b, c$ and $d$, all between 0 and 4. Assume $a+b>0$ and $c+d>0$.

## Output

For every case, tell if X will win, if X will lose, or if the game is a draw.

## Sample input

|  | 4 | 0 | 3 |
| :--- | :--- | :--- | :--- |
| 1 | 0 | 4 | 0 |
| 0 | 1 | 0 | 1 |
| 3 | 0 | 2 | 3 |
| 3 | 3 | 0 | 4 |
| 1 | 1 | 1 | 1 |

## Sample output

## Problem information

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